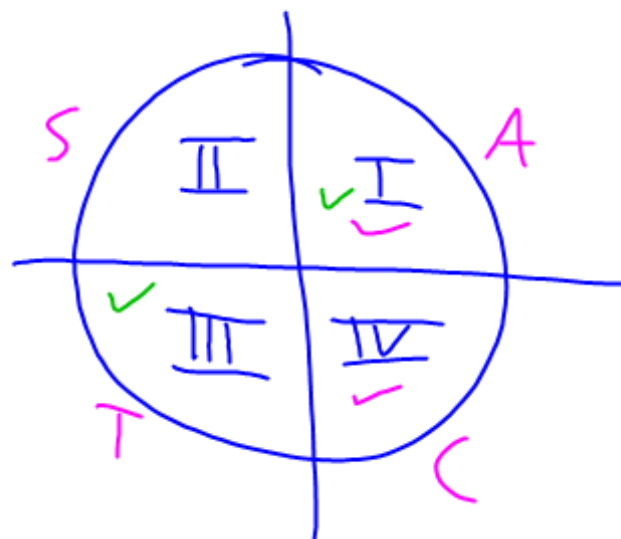


13 in 1.3

$$\sin \theta = \frac{y}{r} \rightarrow \text{pos.}$$

$$\csc \theta = \frac{r}{y} \rightarrow \text{pos.}$$

28-32 in 1.4



1 in 1.4

$$a = 1$$

12 in 1.4

Find  $\sec \theta$  if  $\cos \theta = \frac{3}{2}$   
 can't be bigger than 1

21 in 1.4)

$$\tan \theta = \frac{1}{\cot \theta}$$

$$\tan(3\theta - 4^\circ) = \frac{1}{\cot(5\theta - 8)}$$

$$\tan(3\theta - 4) = \tan(5\theta - 8)$$

$$3\theta - 4 = 5\theta - 8$$

$$4 = 2\theta$$

$$\theta = 2$$

41 in 1.3

$$\sec^2 180^\circ - 3 \sin^2 360^\circ + 2 \cos 180^\circ$$

$$x = -1$$

$$y = 0$$

$$r = 1$$

$$x = 1$$

$$y = 0$$

$$r = 1$$

$$x = -1$$

$$y = 0$$

$$r = 1$$

$$\sec 180^\circ$$

$$(-1)^2$$

$$1 -$$

$$\sin 360^\circ$$

$$3 \cdot (0)^2$$

$$0$$

$$+$$

$$-2$$

$$\cos 180^\circ$$

$$2 \cdot -1$$

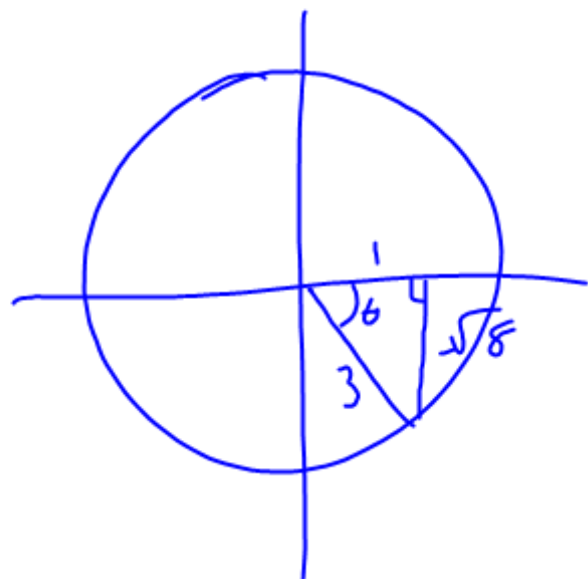
$$= -1$$

55 in 1.4)

Find  $\tan \theta$  if  $\sec \theta = 3$  in Quad IV

$$\downarrow$$

$$\frac{r}{x} \quad \frac{3}{1}$$



$$1^2 + y^2 = 3^2$$

$$y = \sqrt{8}$$

$$\sqrt{4} \cdot \sqrt{2}$$

$$\tan = \frac{y}{x} = -\frac{\sqrt{8}}{1} = -\frac{2\sqrt{2}}{1} = -2\sqrt{2}$$

70 in 1.4

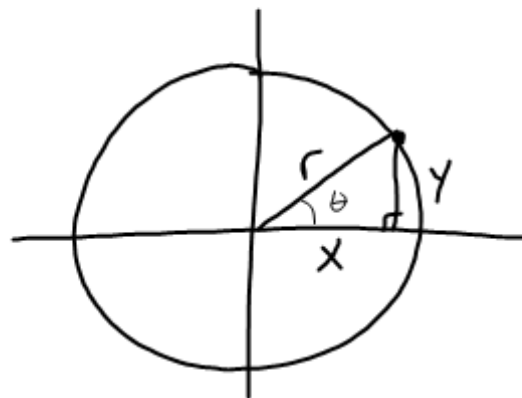
$$\cot \theta = \frac{1}{\tan \theta} = -1.49586$$

$$\rightarrow \tan \theta = \frac{1}{-1.49586}$$

$$\theta = \tan^{-1} \left( \frac{1}{-1.49586} \right)$$

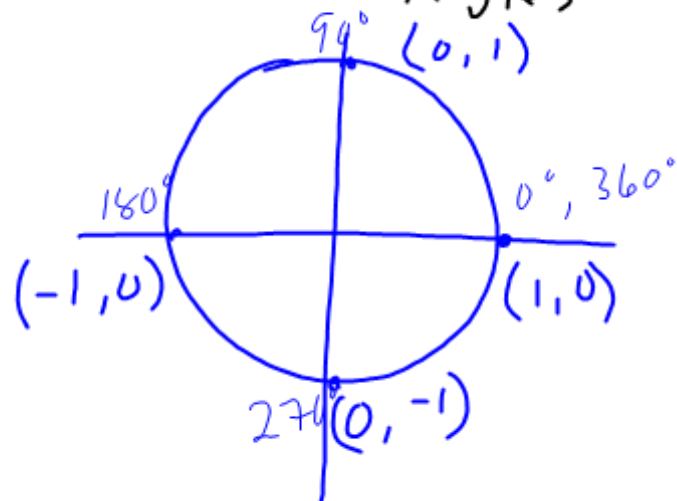
# Ch. 1 Review

## ① Trig Basics



$$\begin{aligned} \sin \theta &= \frac{y}{r} & \csc \theta &= \frac{r}{y} \\ \cos \theta &= \frac{x}{r} & \sec \theta &= \frac{r}{x} \\ \tan \theta &= \frac{y}{x} & \cot \theta &= \frac{x}{y} \end{aligned}$$

## ② Quadrantal Angles



$$\cos \theta = \frac{x}{1} \Rightarrow \underline{\cos \theta = x}$$

$$\sin \theta = \frac{y}{1} \Rightarrow \underline{\sin \theta = y}$$

$$\tan \theta = \frac{y}{x}$$

$$\cot \theta = \frac{x}{y}$$

$$\csc \theta = \frac{1}{y}$$

$$\sec \theta = \frac{1}{x}$$

### ③ Ranges

$$-1 \leq \sin \theta \leq 1$$

$$-1 \leq \cos \theta \leq 1$$

$$-\infty < \tan \theta < \infty$$

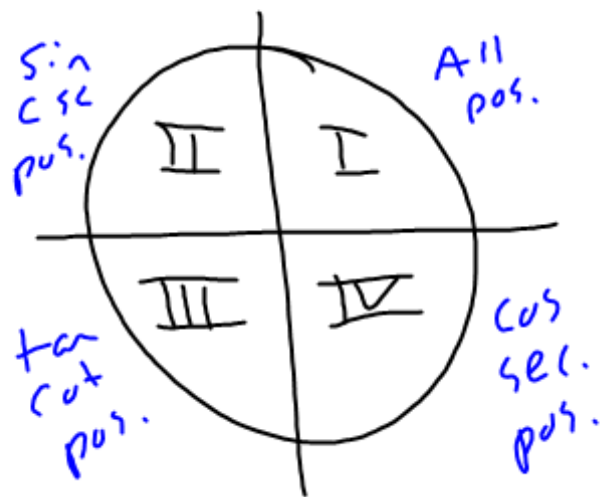


$$\csc \theta \leq -1 \text{ and } 1 \leq \csc \theta$$

$$\sec \theta \leq -1 \text{ and } 1 \leq \sec \theta$$

$$-\infty < \cot \theta < \infty$$

### ④ Signs of Trig Functions



All sin tan csc sec pos

## ⑤ Reciprocal Identities

$$\sin \theta = \frac{1}{\csc \theta}$$

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\cos \theta = \frac{1}{\sec \theta}$$

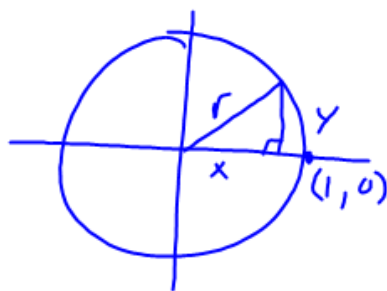
$$\sec \theta = \frac{1}{\cos \theta}$$

$$\tan \theta = \frac{1}{\cot \theta}$$

$$\cot \theta = \frac{1}{\tan \theta}$$



## ⑥ Pythagorean Identities



$$x^2 + y^2 = r^2$$

Divide by  $r^2$

$$\frac{x^2}{r^2} + \frac{y^2}{r^2} = \frac{r^2}{r^2}$$

$$\left(\frac{x}{r}\right)^2 + \left(\frac{y}{r}\right)^2 = 1$$

$$\cos^2 \theta + \sin^2 \theta = 1$$

Divide by  $y^2$

$$\frac{x^2}{y^2} + \frac{y^2}{y^2} = \frac{r^2}{y^2}$$

$$\cot^2 \theta + 1 = \csc^2 \theta$$

Divide by  $x^2$

$$\frac{x^2}{x^2} + \frac{y^2}{x^2} = \frac{r^2}{x^2}$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

## Quotient Identities

$$\frac{\sin \theta}{\cos \theta} = \frac{\frac{y}{r}}{\frac{x}{r}} \Rightarrow \frac{y}{\cancel{r}} \cdot \frac{\cancel{r}}{x} = \frac{y}{x} = \tan \theta$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta}$$

$\Rightarrow$  Sect. 1.1 #63-68(2)

Sect. 1.2 #62

Sect. 1.3 #27, 42, 60

Sect. 1.4 #24, 57, 60

Cl. Review p.39 #1-3, 6, 8, 10, 12, 16, 18, 24-27,  
40, 44